

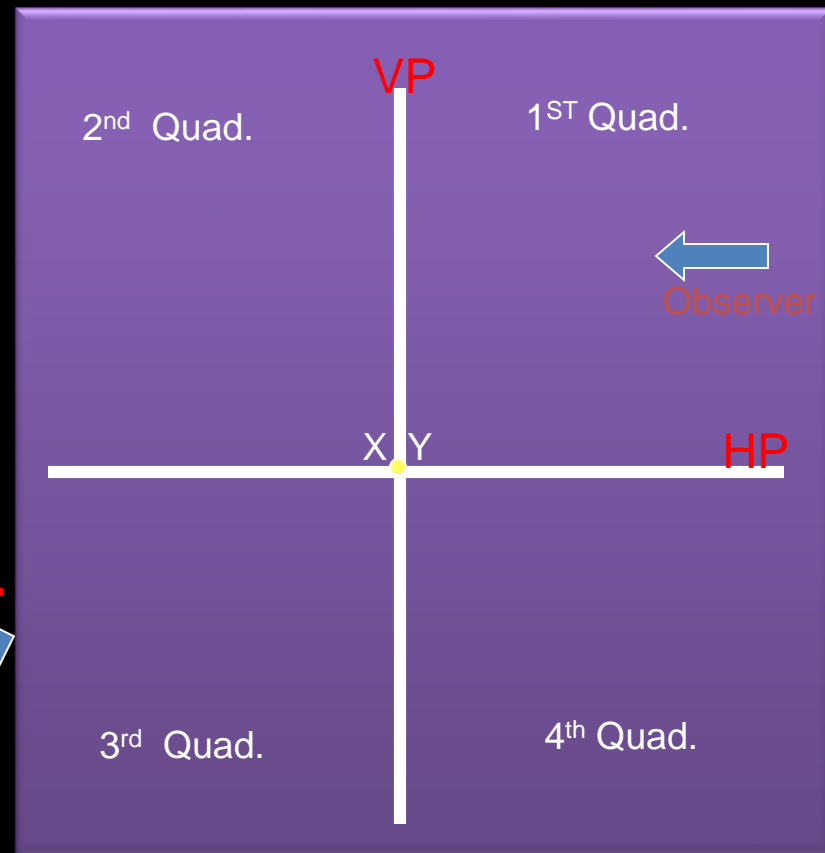
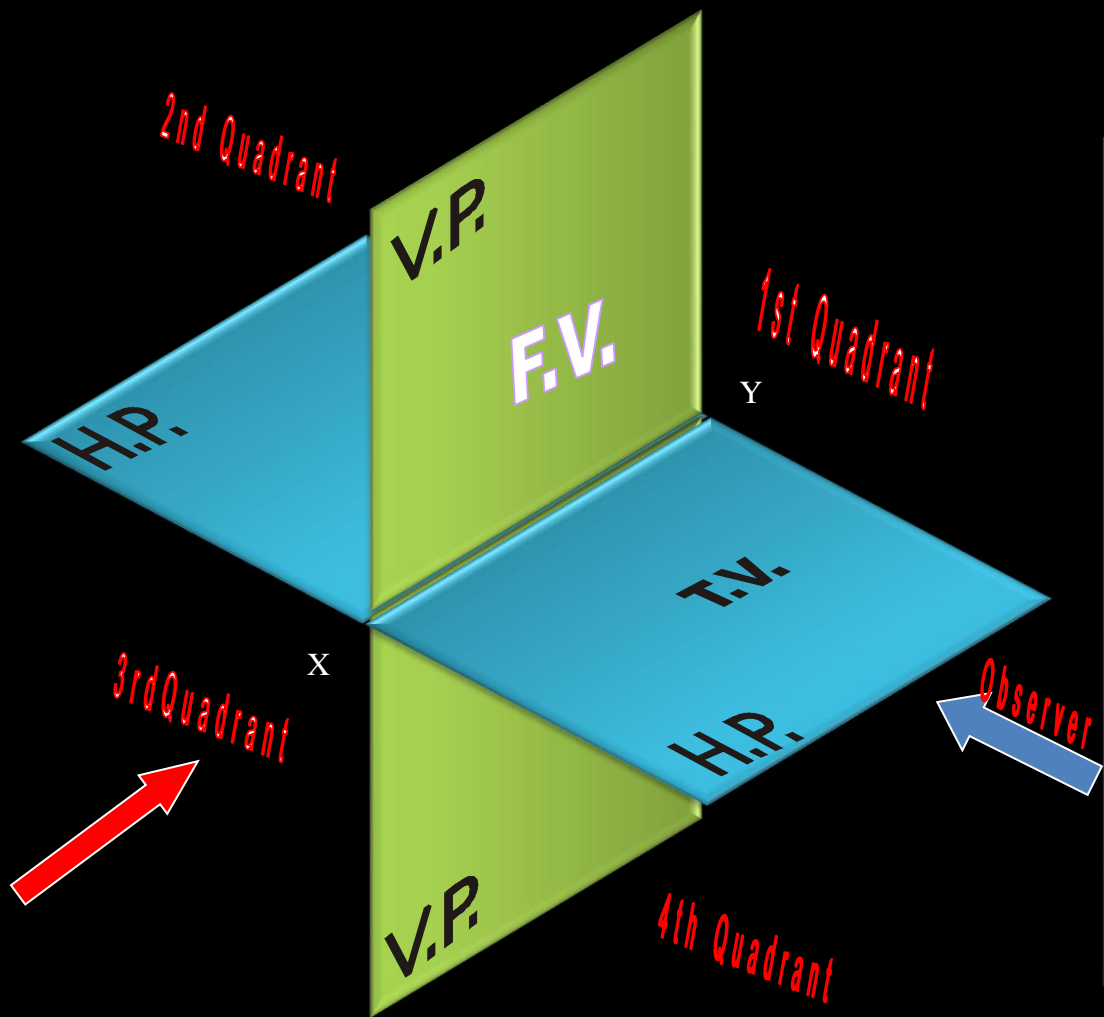
# Projection of point and line

# NOTATIONS

FOLLOWING NOTATIONS SHOULD BE FOLLOWED WHILE NAMEING DIFFERENT VIEWS IN ORTHOGRAPHIC PROJECTIONS.

OBJECT	POINT A	LINE AB
IT'S TOP VIEW	a	a b
IT'S FRONT VIEW	a'	a' b'
IT'S SIDE VIEW	a''	a'' b''

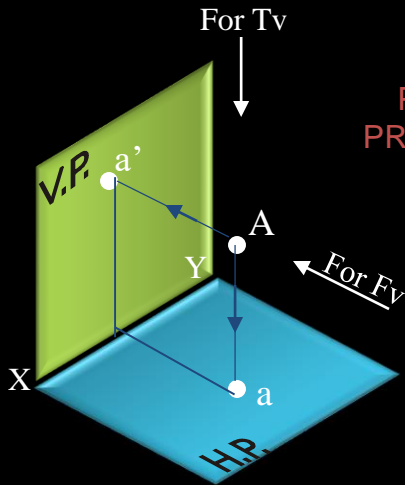
*SAME SYSTEM OF NOTATIONS SHOULD BE FOLLOWED  
INCASE NUMBERS, LIKE 1, 2, 3 – ARE USED.*



THIS QUADRANT PATTERN,  
 IF OBSERVED ALONG X-Y LINE ( IN RED ARROW DIRECTION )  
 WILL EXACTLY APPEAR AS SHOWN ON RIGHT SIDE AND HENCE,  
 IT IS FURTHER USED TO UNDERSTAND ILLUSTRATION PROPERLY.

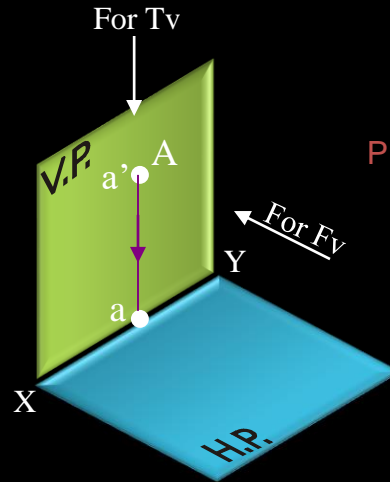
# PROJECTIONS OF A POINT IN FIRST QUADRANT.

POINT A ABOVE HP  
& IN FRONT OF VP



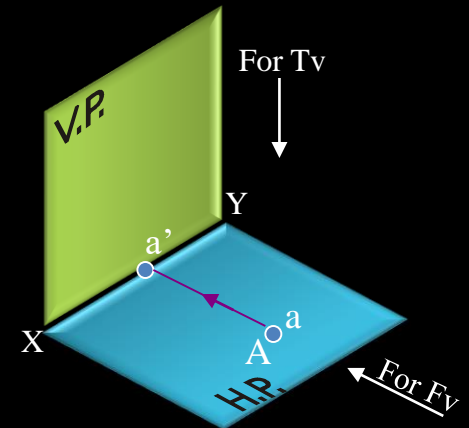
PICTORIAL  
PRESENTATION

POINT A ABOVE HP  
& IN VP



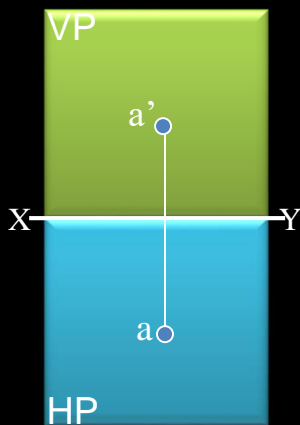
PICTORIAL  
PRESENTATION

POINT A IN HP  
& IN FRONT OF VP

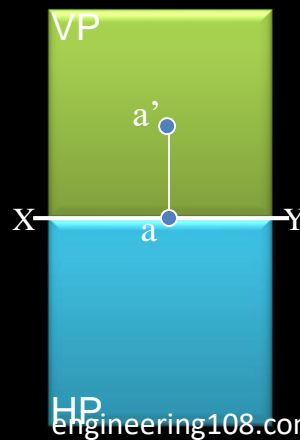


ORTHOGRAPHIC PRESENTATIONS  
OF ALL ABOVE CASES.

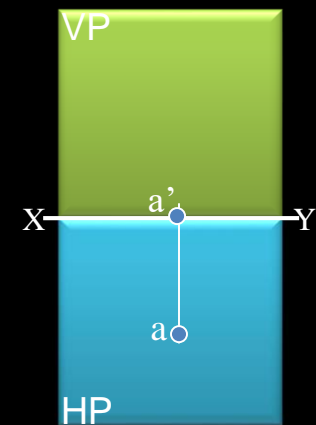
*Fv above xy,  
Tv below xy.*



*Fv above xy,  
Tv on xy.*



*Fv on xy,  
Tv below xy.*





Easy Education

# PROJECTIONS OF STRAIGHT LINES.

INFORMATION REGARDING A LINE *means*  
IT'S LENGTH,  
POSITION OF IT'S ENDS WITH HP & VP  
IT'S INCLINATIONS WITH HP & VP WILL BE GIVEN.  
AIM:- TO DRAW IT'S PROJECTIONS - MEANS FV & TV.

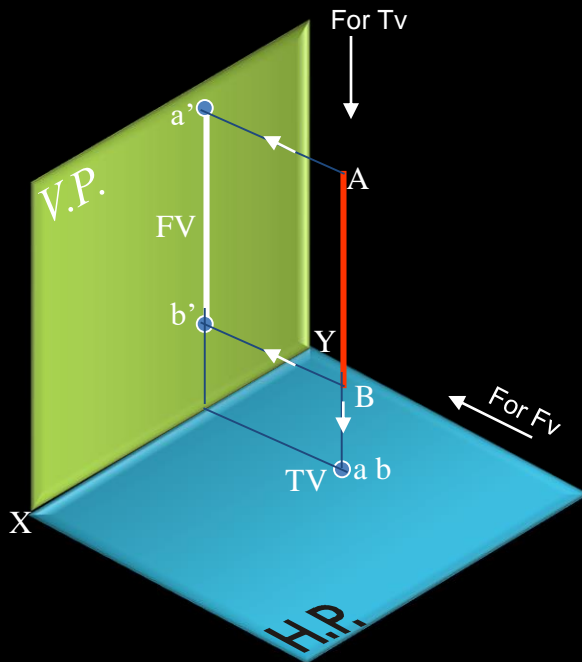
## **SIMPLE CASES OF THE LINE**

1. A VERTICAL LINE ( LINE PERPENDICULAR TO HP & // TO VP)
2. LINE PARALLEL TO BOTH HP & VP.
3. LINE INCLINED TO HP & PARALLEL TO VP.
4. LINE INCLINED TO VP & PARALLEL TO HP.
5. LINE INCLINED TO BOTH HP & VP.

**STUDY ILLUSTRATIONS GIVEN ON NEXT PAGE  
SHOWING CLEARLY THE NATURE OF FV & TV  
OF LINES LISTED ABOVE AND NOTE RESULTS.**

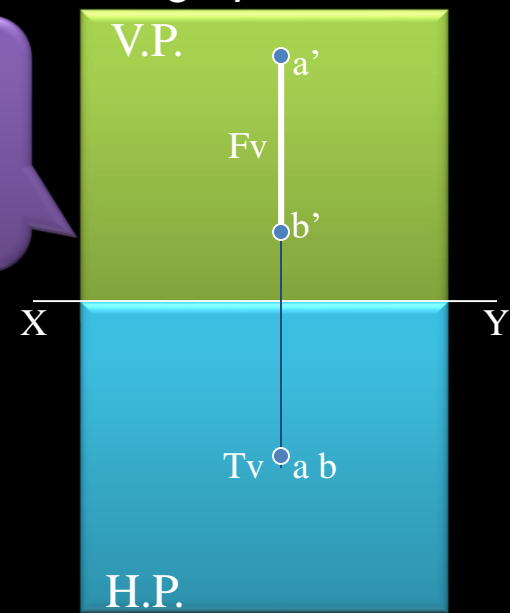
1.

A Line perpendicular to Hp & // to Vp



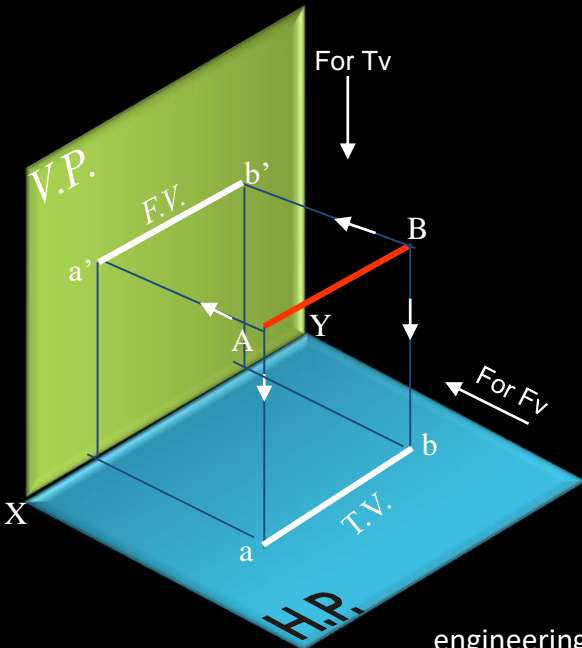
Fv is a vertical line Showing True Length & Tv is a point.

Orthographic Pattern



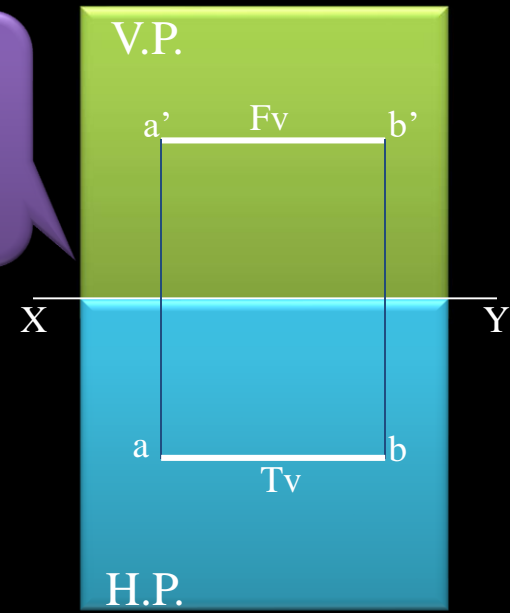
2.

A Line // to Hp & // to Vp



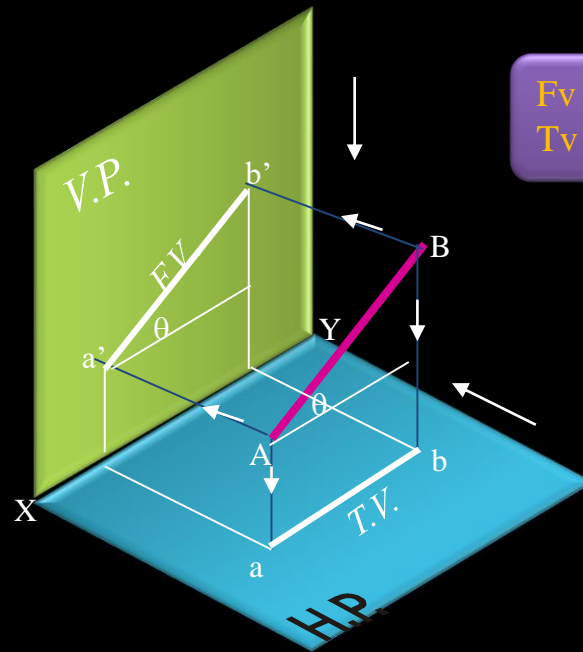
Fv & Tv both are // to xy & both show T.L.

Orthographic Pattern

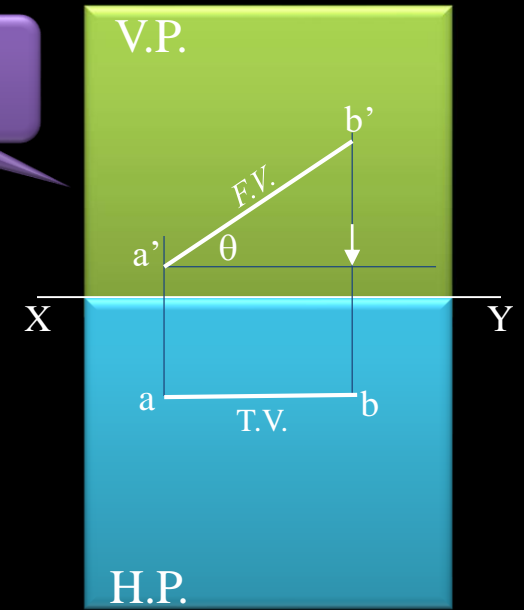


3.

A Line inclined to Hp and parallel to Vp



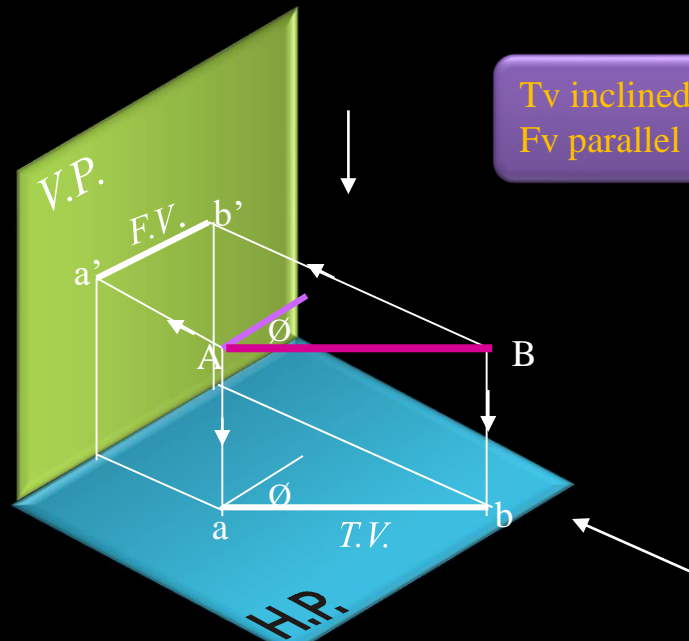
Fv inclined to xy  
Tv parallel to xy.



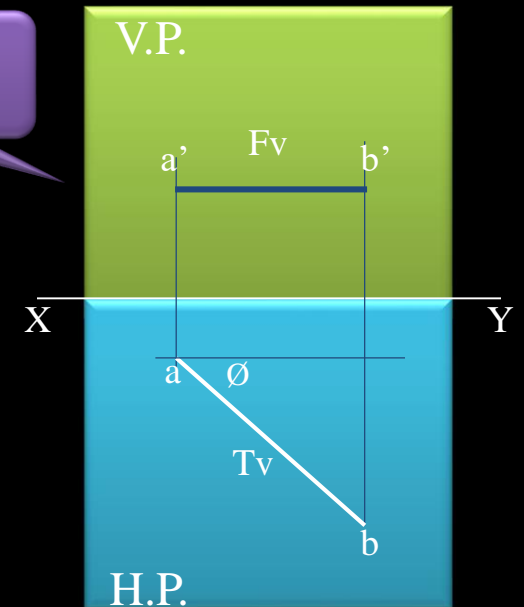
Orthographic Projections

4.

A Line inclined to Vp and parallel to Hp



Tv inclined to xy  
Fv parallel to xy.

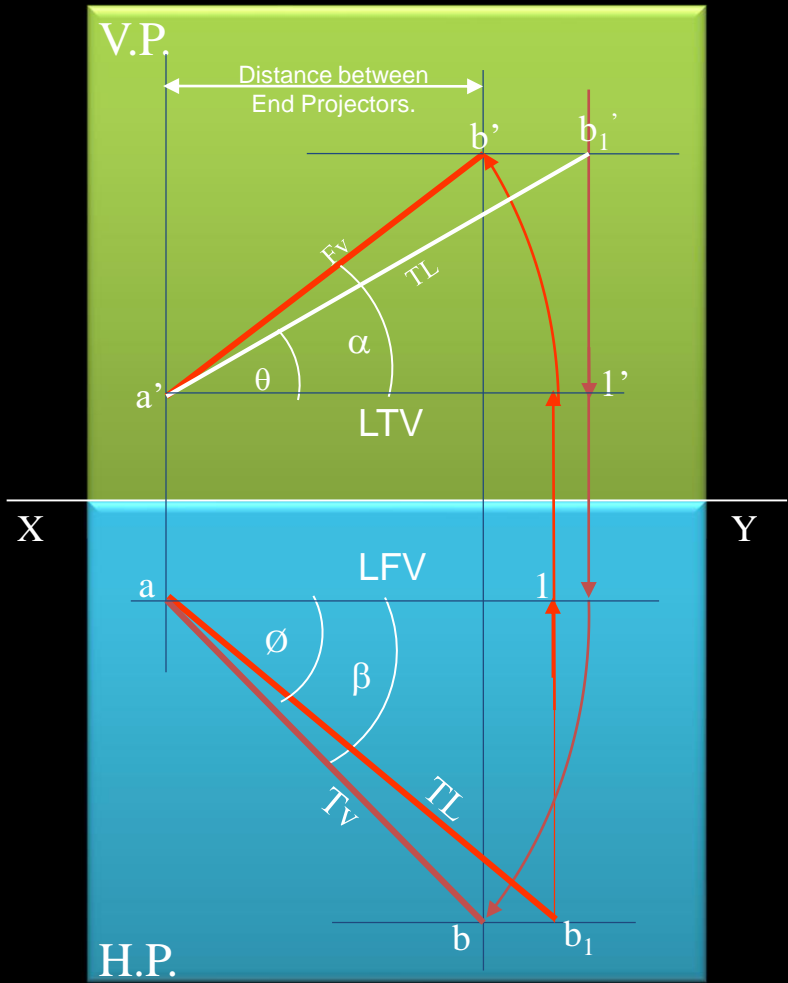






Easy Education

The most important diagram showing graphical relations among all important parameters of this topic. Study and memorize it as a *CIRCUIT DIAGRAM* And use in solving various problems.



- 1) True Length ( TL ) –  $a'b_1'$  &  $ab_1$
- 2) Angle of TL with Hp -  $\theta$
- 3) Angle of TL with Vp –  $\phi$
- 4) Angle of FV with xy –  $\alpha$
- 5) Angle of TV with xy –  $\beta$
- 6) LTV (length of FV) – Component (a-1)
- 7) LFV (length of TV) – Component ( $a'-1'$ )
- 8) Position of A- Distances of a & a' from xy
- 9) Position of B- Distances of b & b' from xy
- 10) FV projection –  $ab'$  and TV projection -  $ab$

Important  
TEN parameters  
to be remembered  
with Notations  
used here onward

*NOTE this*  
 $\theta$  &  $\alpha$  Construct with  $a'$   
 $\phi$  &  $\beta$  Construct with  $a$   
 $b'$  &  $b_1'$  on same locus.  
 $b$  &  $b_1$  on same locus.

*Also Remember*  
 True Length is never rotated. It's horizontal component is drawn & it is further rotated to locate view.  
 Views are always rotated, made horizontal & further extended to locate TL,  $\theta$  &  $\phi$

## GROUP (A)

### GENERAL CASES OF THE LINE INCLINED TO BOTH HP & VP ( based on 10 parameters).

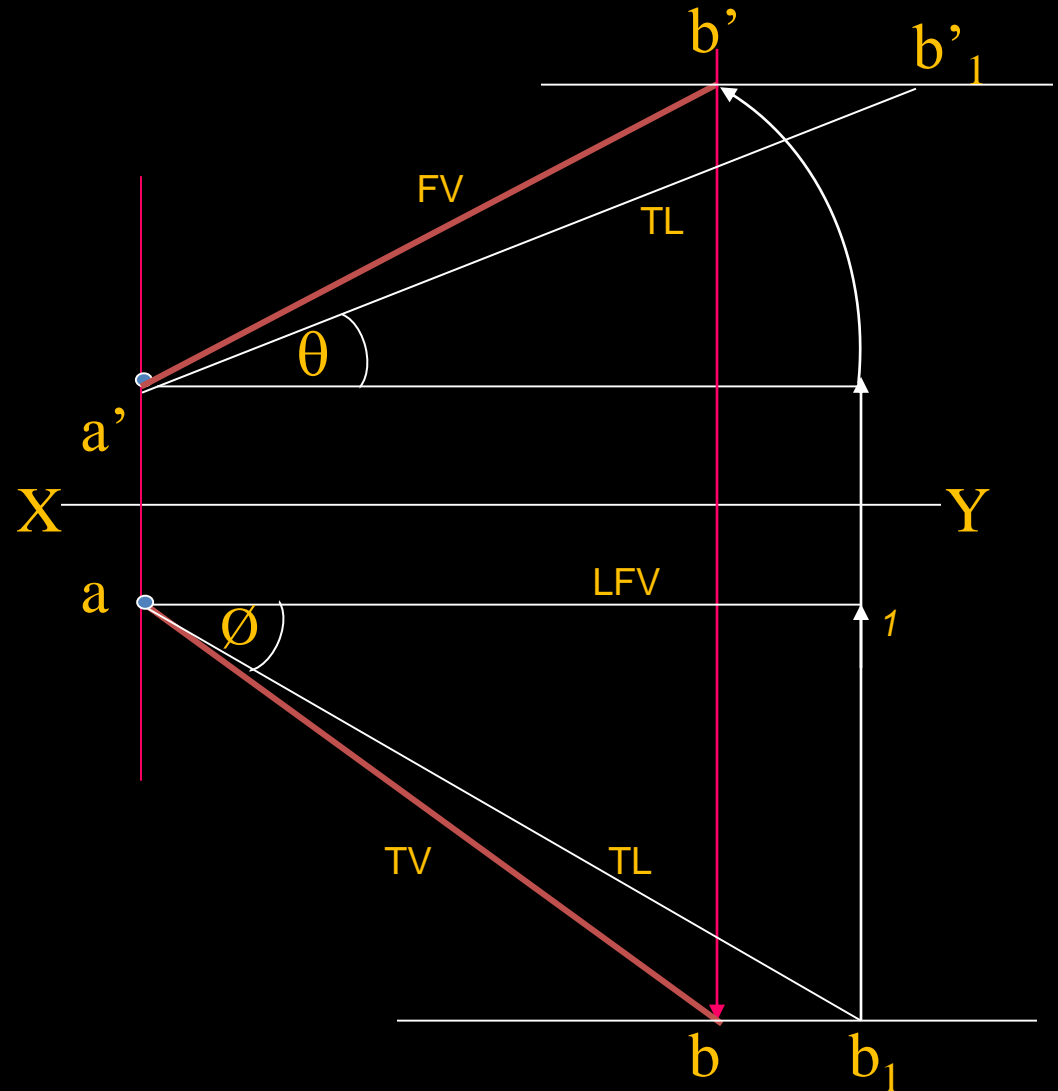
#### PROBLEM 1

Line AB is 75 mm long and it is  $30^\circ$  &  $40^\circ$  Inclined to Hp & Vp respectively.  
End A is 12mm above Hp and 10 mm in front of Vp.

Draw projections. Line is in 1<sup>st</sup> quadrant.

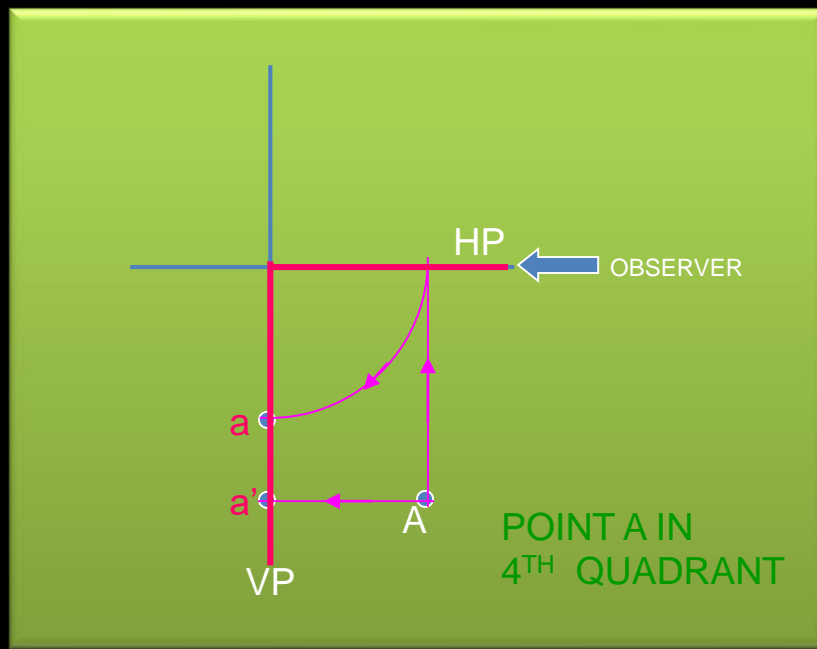
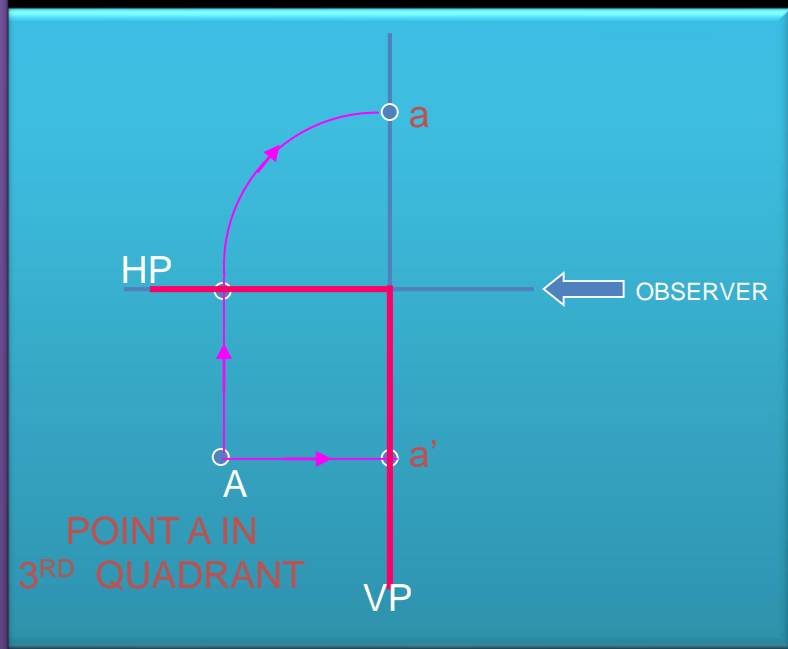
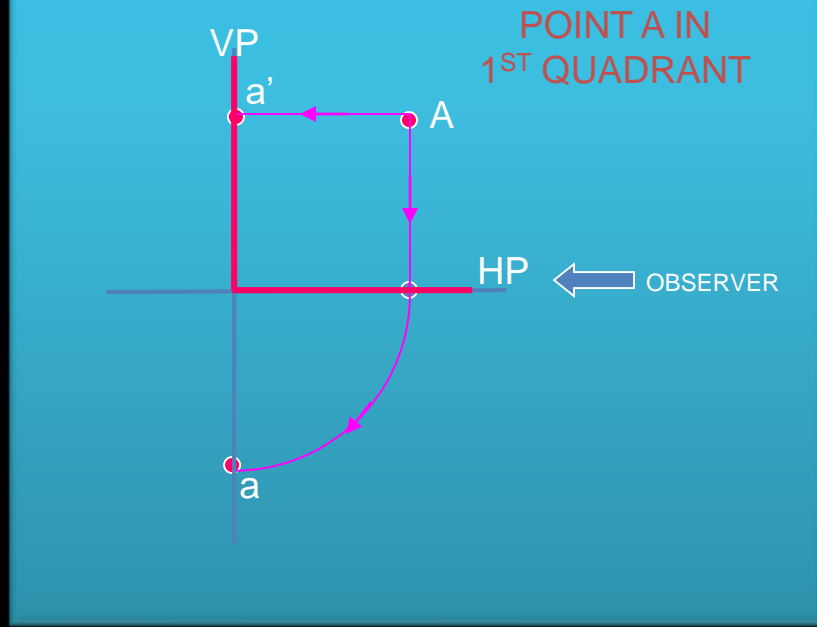
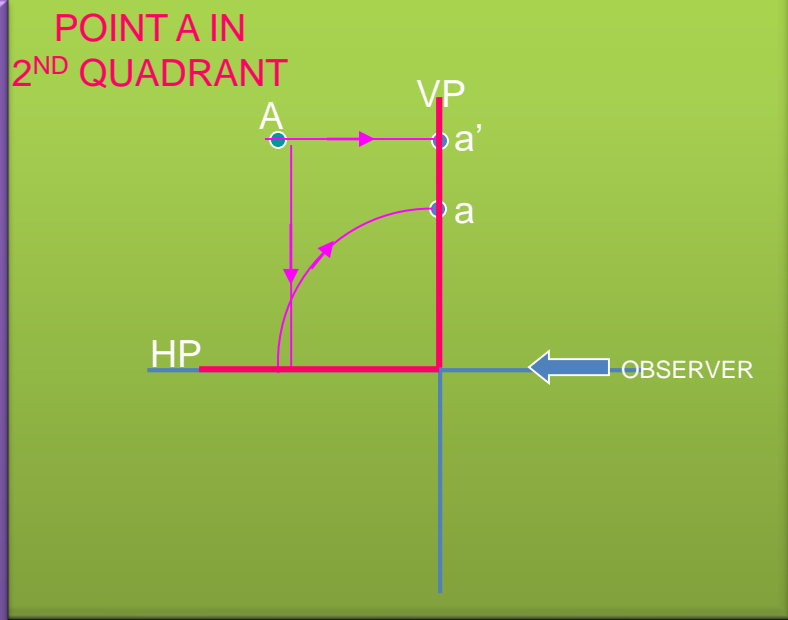
#### SOLUTION STEPS:

- 1) Draw xy line and one projector.
- 2) Locate  $a'$  12mm above xy line &  $a$  10mm below xy line.
- 3) Take  $30^\circ$  angle from  $a'$  &  $40^\circ$  from  $a$  and mark TL i.e. 75mm on both lines. Name those points  $b_1'$  and  $b_1$  respectively.
- 4) Join both points with  $a'$  and  $a$  resp.
- 5) Draw horizontal lines (Locus) from both points.
- 6) Draw horizontal component of TL a  $b_1$  from point  $b_1$  and name it 1. ( the length  $a-1$  gives length of Fv as we have seen already.)
- 7) Extend it up to locus of  $a'$  and rotating  $a'$  as center locate  $b'$  as shown. Join  $a' b'$  as Fv.
- 8) From  $b'$  drop a projector down ward & get point  $b$ . Join  $a$  &  $b$  i.e. Tv.



Point A is Placed In different quadrants and it's Fv & Tv are brought in same plane for Observer to see clearly. Fv is visible as it is a view on VP. But as Tv is a view on Hp, it is rotated downward 90°, In clockwise direction. The In front part of Hp comes below xy line and the part behind Vp comes above.

Observe and note the process.

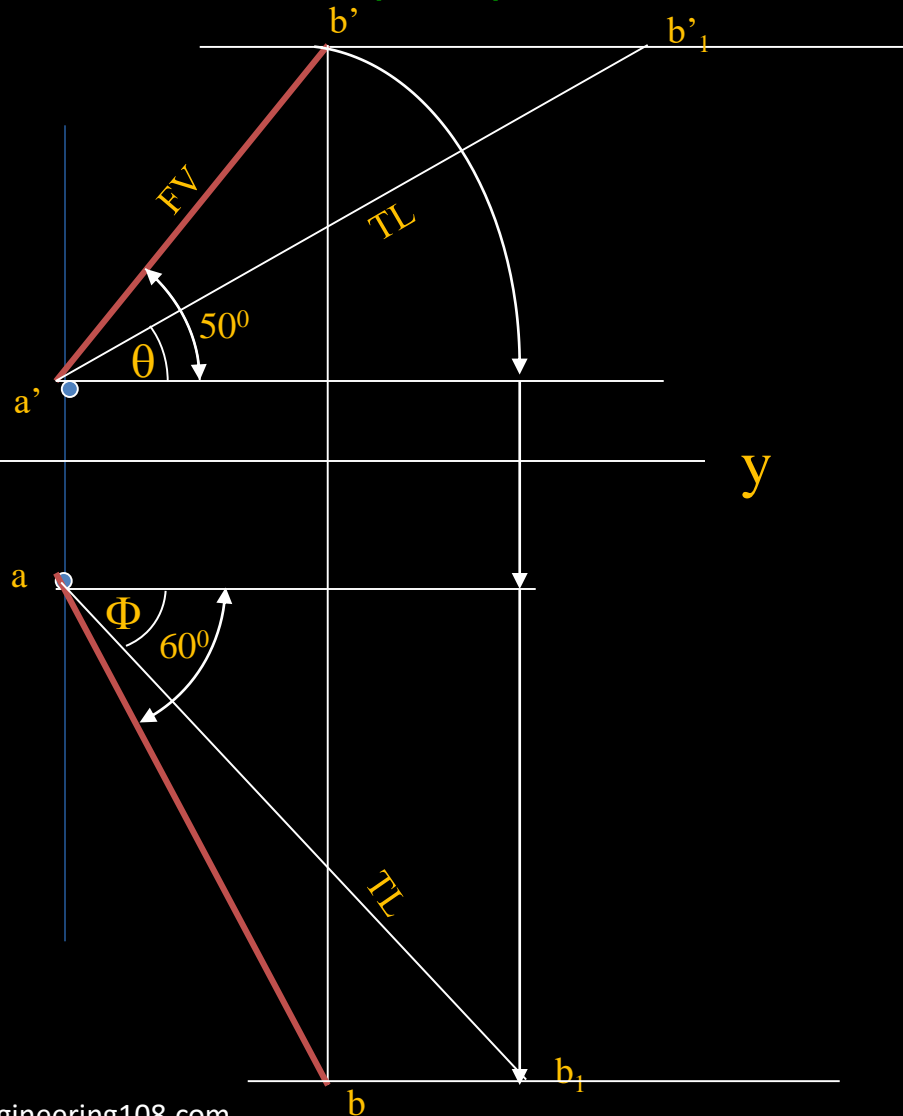




PROBLEM 3 - Fv of line AB is  $50^\circ$  inclined to xy and measures 55 mm long while it's Tv is  $60^\circ$  inclined to xy line. If end A is 10 mm above Hp and 15 mm in front of Vp, draw it's projections, find TL, inclinations of line with Hp & Vp.

**SOLUTION STEPS:**

1. Draw xy line and one projector.
2. Locate a' 10 mm above xy and a 15 mm below xy line. **X**
3. Draw locus from these points.
4. Draw Fv  $50^\circ$  to xy from a' and mark b' Cutting 55mm on it.
5. Similarly draw Tv  $60^\circ$  to xy from a & drawing projector from b' Locate point b and join a b.
6. Then rotating views as shown, locate True Lengths  $ab_1$  &  $a'b_1'$  and their angles with Hp and Vp.









GROUP (B)  
PROBLEMS INVOLVING TRACES OF THE LINE.

TRACES OF THE LINE:-

THESE ARE THE POINTS OF INTERSECTIONS OF A LINE ( OR IT'S EXTENSION ) WITH RESPECTIVE REFERENCE PLANES.

*A LINE ITSELF OR IT'S EXTENSION, WHERE EVER TOUCHES H.P., THAT POINT IS CALLED TRACE OF THE LINE ON H.P.( IT IS CALLED H.T.)*

*SIMILARLY, A LINE ITSELF OR IT'S EXTENSION, WHERE EVER TOUCHES V.P., THAT POINT IS CALLED TRACE OF THE LINE ON V.P.( IT IS CALLED V.T.)*

*V.T.:- It is a point on  $V_p$ .  
Hence it is called  $F_v$  of a point in  $V_p$ .  
Hence it's  $T_v$  comes on XY line.( Here onward named as 'V' )*

*H.T.:- It is a point on  $H_p$ .  
Hence it is called  $T_v$  of a point in  $H_p$ .  
Hence it's  $F_v$  comes on XY line.( Here onward named as 'h' )*

### STEPS TO LOCATE HT.

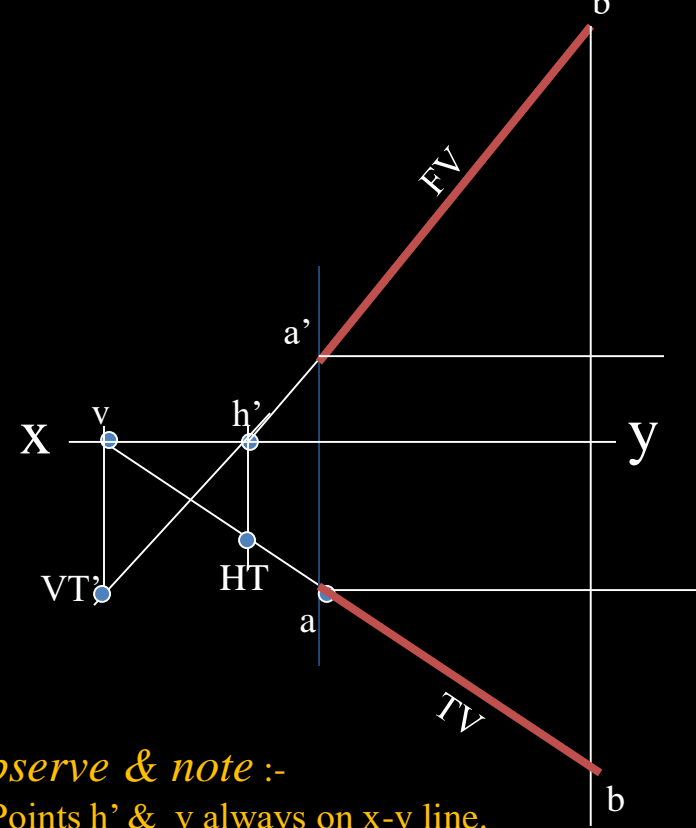
(WHEN PROJECTIONS ARE GIVEN.)

1. Begin with FV. Extend FV up to XY line.
2. Name this point  $h'$   
(as it is a Fv of a point in Hp)
3. Draw one projector from  $h'$ .
4. Now extend Tv to meet this projector.  
This point is HT

### STEPS TO LOCATE VT.

(WHEN PROJECTIONS ARE GIVEN.)

1. Begin with TV. Extend TV up to XY line.
2. Name this point  $v$   
(as it is a Tv of a point in Vp)
3. Draw one projector from  $v$ .
4. Now extend Fv to meet this projector.  
This point is VT



*Observe & note :-*

1. Points  $h'$  &  $v$  always on x-y line.
2.  $VT'$  &  $v$  always on one projector.
3.  $HT$  &  $h'$  always on one projector.
4.  $FV - h' - VT'$  always co-linear.
5.  $TV - v - HT$  always co-linear.

**PROBLEM 1 :-** Fv of line AB makes  $45^\circ$  angle with XY line and measures 60 mm. Line's Tv makes  $30^\circ$  with XY line. End A is 15 mm above Hp and it's VT is 10 mm below Hp. Draw projections of line AB, determine inclinations with Hp & Vp and locate HT, VT.

**SOLUTION STEPS:-**

Draw xy line, one projector and locate fv  $a'$  15 mm above xy.

Take  $45^\circ$  angle from  $a'$  and marking 60 mm on it locate point  $b'$ .

Draw locus of VT, 10 mm below xy & extending Fv to this locus locate VT. as fv-h'-vt' lie on one st.line.

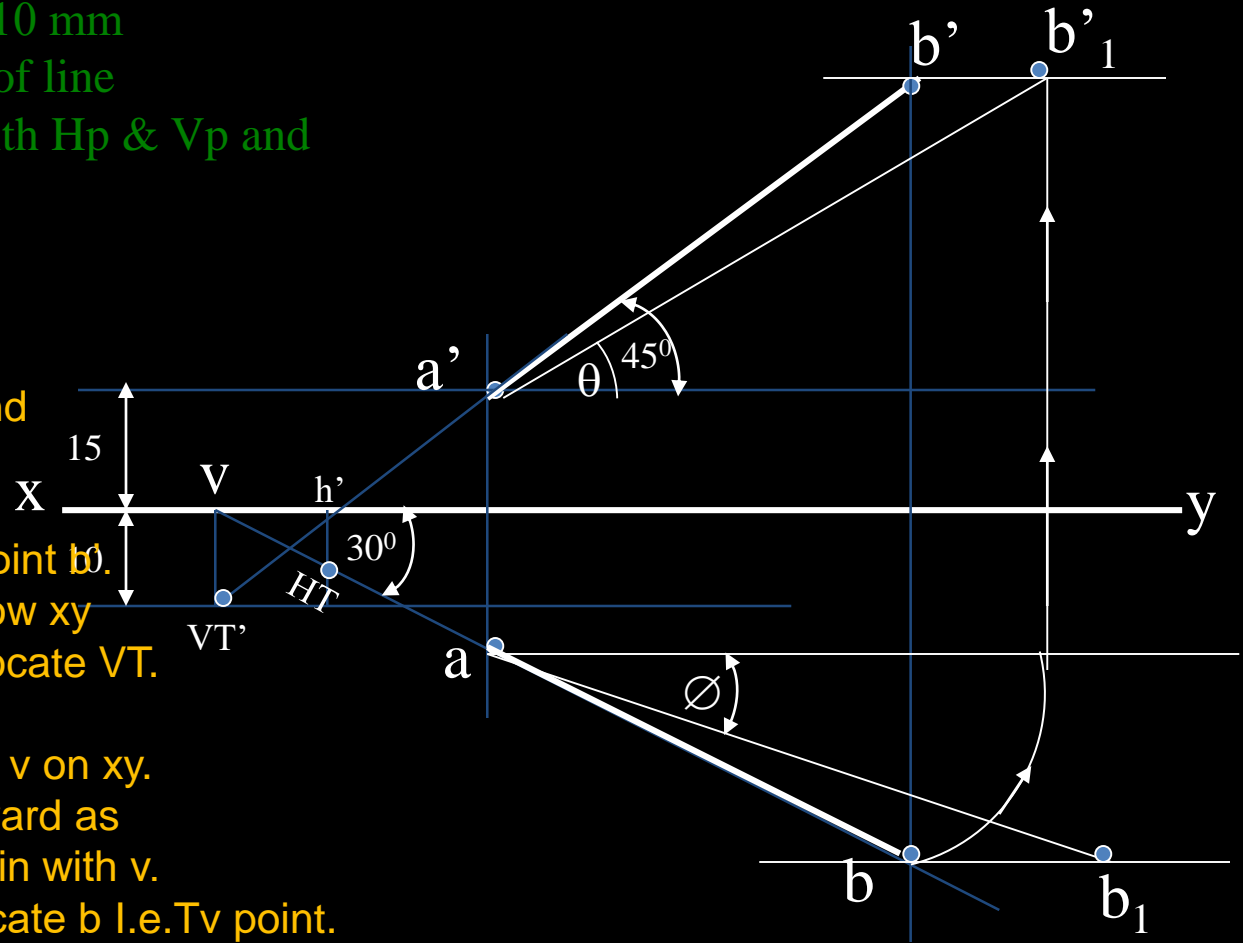
Draw projector from vt, locate v on xy.

From v take  $30^\circ$  angle downward as Tv and it's inclination can begin with v.

Draw projector from  $b'$  and locate b i.e. Tv point.

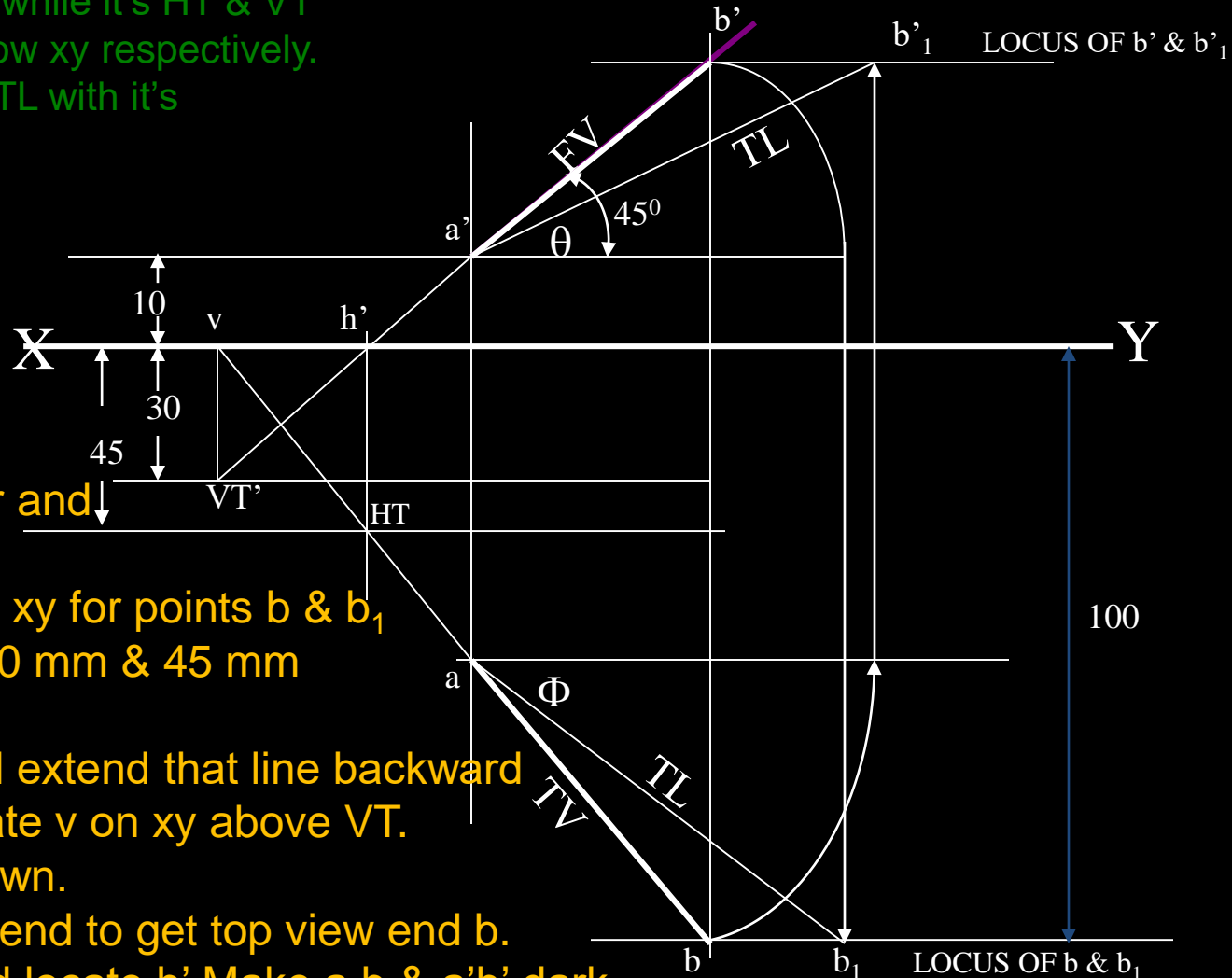
Now rotating views as usual TL and it's inclinations can be found.

Name extension of Fv, touching xy as  $h'$  and below it, on extension of Tv, locate HT.



## PROBLEM 2

One end of line AB is 10mm above Hp and other end is 100 mm in-front of Vp. It's Fv is  $45^\circ$  inclined to xy while it's HT & VT are 45mm and 30 mm below xy respectively. Draw projections and find TL with it's inclinations with Hp & VP.



### SOLUTION STEPS:-

Draw xy line, one projector and locate a' 10 mm above xy.

Draw locus 100 mm below xy for points b & b<sub>1</sub>

Draw loci for VT and HT, 30 mm & 45 mm below xy respectively.

Take  $45^\circ$  angle from a' and extend that line backward to locate h' and VT, & Locate v on xy above VT.

Locate HT below h' as shown.

Then join v – HT – and extend to get top view end b.

Draw projector upward and locate b' Make a b & a'b' dark.

Now as usual rotating views find TL and it's inclinations.